Tunable Ultrafast Thermal Relaxation in Graphene Measured by Continuous-Wave Photomixing

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(Received 18 July 2016; published 13 December 2016)

Hot electron effects in graphene are significant because of graphene’s small electronic heat capacity and weak electron-phonon coupling, yet the dynamics and cooling mechanisms of hot electrons in graphene are not completely understood. We describe a novel photocurrent spectroscopy method that uses the mixing of continuous-wave lasers in a graphene photothermal detector to measure the frequency dependence and nonlinearity of hot-electron cooling in graphene as a function of the carrier concentration and temperature. The method offers unparalleled sensitivity to the nonlinearity, and probes the ultrafast cooling of hot carriers with an optical fluence that is orders of magnitude smaller than in conventional time-domain methods, allowing for accurate characterization of electron-phonon cooling near charge neutrality. Our measurements reveal that near the charge neutral point the nonlinear power dependence of the electron cooling is dominated by disorder-assisted collisions, while at higher carrier concentrations conventional momentum-conserving cooling prevails in the nonlinear dependence. The relative contribution of these competing mechanisms can be electrostatically tuned through the application of a gate voltage—an effect that is unique to graphene.

DOI: 10.1103/PhysRevLett.117.257401

When graphene absorbs electromagnetic radiation, its electrons heat up and produce a measurable thermoelectric response, even at room temperature. Because of graphene’s gapless dispersion relation, small electronic heat capacity, and anomalously weak electron-phonon coupling, this photothermal detection mechanism is broadband (from dc to visible), highly sensitive, and fast [1–5]. The speed, temperature dependence, and power dependence of these detectors depend critically upon how fast and by what mechanisms the hot carriers relax [6–8]. Two primary cooling mechanisms have been identified: supercollision cooling, in which disorder-assisted scattering allows for non-momentum conserving transitions, and conventional momentum conserving electron-phonon cooling [6,7,9–14]. Evidence for conventional momentum-conserving cooling (which is linear with temperature) has been observed only at low temperatures in high-quality graphene [8]. In experimental measurements, the cooling process is inferred from how the photothermal response depends on temperature, power, or time for either pulsed or continuous-wave illumination. Time-domain methods that are used to study thermal relaxation dynamics typically employ intense optical pulses, which significantly disturb the electron temperature, and can in some cases excite higher energy optical phonons in addition to acoustic phonons [7,15–17]. Moreover, as we show here, the factors that govern the power dependence of the photothermal response can be different from those that determine the cooling rate. It has been shown that, uniquely in graphene, the relative strength of the two competing cooling channels can be controlled by the carrier concentration [6,8,12].

Here, we employ a new nonlinear photomixing method to simultaneously quantify the nonlinearity in the photothermal response and the carrier-density dependence of electron cooling in graphene. This method easily distinguishes between sublinear and superlinear power dependence, which indicate supercollision cooling and conventional cooling, respectively. Our measurements show that while supercollision cooling dominates the nonlinear response near the charge neutral point, at higher carrier densities, conventional cooling is the dominant contribution to the nonlinearity. Furthermore, we show that when two detuned near-IR lasers co-illuminate the graphene, the resulting dc photovoltage depends upon their heterodyne difference frequency. This enables the direct measurement of the electron cooling rate in the frequency domain with orders of magnitude weaker optical excitation (smaller temperature rise) than traditional time-domain methods, by simply tuning the wavelength of one of the continuous-wave lasers.

Figure 1(a) depicts the heterodyne photomixing setup used here to characterize the photothermal response of graphene. Two fiber-coupled continuous-wave near-IR
lasers, one wavelength tunable ($\lambda_1 = 1540–1565$ nm) and one at fixed wavelength ($\lambda_2 = 1545$ nm), were amplified, spatially combined, polarized, and focused using an aspheric lens to a 3 $\mu$m spot on the graphene channel. The position of the focused beam was chosen to maximize the photovoltage, which occurs when the beam is focused close to one of the metal contacts, and the carrier density of graphene is altered by applying an electrostatic voltage ($V_g$) between the doped silicon substrate and graphene.

FIG. 1. Diagram of heterodyne photomixing experiment. (a) Two near-IR continuous-wave beams, one with a tunable wavelength, are modulated at two different frequencies $f_1$ and $f_2$, then overlapped and focused down to the graphene photodetector. The photovoltages produced by laser 1 ($V_1$) and the mixing of two beams ($V_\Delta$) are detected at the modulation frequencies $f_1$ and $f_2$, respectively. (b) Diagram of the HBN-encapsulated graphene (top) and exfoliated graphene (bottom) photodetector devices. The optical beams are illuminated close to one of the metal contacts, and the carrier density of graphene is altered by applying an electrostatic voltage ($V_g$) between the doped silicon substrate and graphene.

which we estimate the total absorbed intensity to be $I$.

To better elucidate the role of disorder, we considered two different graphene detectors shown in Fig. 1(b): one using an edge-contacted hexagonal boron nitride (HBN) encapsulated graphene channel [20,21], and a second fabricated from an unencapsulated exfoliated flake [5]. The Supplemental Material [33] details the fabrication and dc electrical characterization of the devices (Sec. S4).

The electron temperature $T$ in the graphene evolves according to the nonlinear differential equation [6,9,22]

$$\alpha T \frac{dT}{dt} + \beta_1(T - T_L) + \beta_3(T^3 - T_L^3) = I(t),$$

where $T_L$ is the lattice temperature, $\alpha T$ is the specific heat of the graphene carriers, the coefficients $\beta_1$ and $\beta_3$ are the rate coefficients for the conventional and supercollision cooling mechanisms, respectively, and $I(t)$ is the absorbed near-infrared optical intensity. For the two-laser illumination shown in Fig. 1(a), the absorbed intensity is $I(t) = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \Omega t$, where $I_1$ and $I_2$ represent the absorbed intensities of lasers 1 and 2, respectively, and $\Omega \equiv 2\pi(\lambda_1^{-1} - \lambda_2^{-1})$ is their heterodyne difference frequency.

It is assumed that the electrons are in the degenerate regime ($E_F \gg k_BT$), and that the electron-electron collisions are fast enough ($\tau_{ee} \gg \Omega$) to allow the temperature of the electron gas to be well defined [9,23]. The hot-electron diffusion length is $\xi = (\kappa / \gamma \alpha T)^{1/2} = v_F(\Gamma)^{-1/2}$, where $\kappa$ is the electronic thermal conductivity, $\Gamma$ is the carrier scattering rate, and the Wiedemann-Franz law was used in the second equality. Even for the encapsulated device considered here, by estimating $\Gamma$ from dc measurements in Fig. S3, we estimate that 500 nm < $\xi$ < 1.5 $\mu$m, which is smaller than the optical beam size employed. We therefore ignore spatial inhomogeneity in $I(t)$ and the thermal diffusion of hot carriers out of the laser beam.

The three model parameters $\alpha$, $\beta_1$, and $\beta_3$ appearing in Eq. (1) depend implicitly on the Fermi level $E_F$ (determined by gating) and the disorder mean-free path $l$ (related to the quality of the graphene) as $\alpha = 2\pi k_F^2 E_F / (3\hbar^2 v_F^2)$, $\beta_1 = V_D^2 \kappa E_F k_B / (2\pi \rho \hbar^2 v_F^2)$, $\beta_3 = \zeta(3) V_D^2 E_F k_B^3 / (\pi^2 \rho \hbar^2 v_F^2 l^3)$, where $v_F$ is the Fermi velocity, $\rho$ is the areal mass density, $s$ is the speed of sound in graphene, $\zeta(3) \approx 1.202$ is the Riemann zeta function, and $V_D$ is the acoustic deformation potential. We note that the substrate surface polar phonons may also play a role in hot carrier diffusion of hot carriers out of the laser beam.

The resulting photothermoelectric voltage $V$ produced by the Seebeck effect is then related to the electron temperature by $V = rT(T - T_L)$, where $rT$ is the Seebeck coefficient of graphene [2,28]. This nonlinear relationship between temperature and photovoltage could be generalized to include a nonlinearity in the Seebeck
coefficient [29,30], but the temperature dependence and power dependence of the observed nonlinearity indicate that this effect is small in comparison to the nonlinearity in cooling. Although other photoresponse mechanisms, such as the photoelectric effect [31], might also contribute to the graphene photoresponse, a photothermal model can adequately describe the photoresponse at the graphene-metal interface [5,13,32].

Equation (1) can be solved using a power series expansion (Supplemental Material [33], Sec. S1), and the resulting dc photovoltage is found to be

\[
V(I_1, I_2) = a_1(I_1 + I_2) + a_2(I_1^2 + I_2^2) - a_3(I_1^3 + I_2^3)
\]

\[
+ 2a_2I_1I_2\left(1 + \frac{\beta_1}{\Omega^2 + \gamma^2}\right)
\]

\[
- 3a_3I_1I_2(I_1 + I_2)\left(1 + \frac{2\beta_3}{\Omega^2 + \gamma^2}\right),
\]

where \(\gamma \equiv (\beta_1 + 3\beta_3T_L^2)/\alpha T_L\) is the linearized cooling rate from both mechanisms. The coefficients \(a_1, a_2,\) and \(a_3\) are given by

\[
a_1 = \frac{r}{\alpha \gamma}, \quad a_2 = \frac{r\beta_1}{(\alpha \gamma T_L)^3}, \quad a_3 = \frac{3r\beta_3^2}{T_L^2 \alpha^5 \gamma^3}.\]

The final two terms in Eq. (2), which contain the factor \(I_1I_2\), represent a nonlinear interaction of the two beams, which occurs only when both beams are present. In order to sensitively detect only these mixing products, we employ a double-modulation configuration in which laser 1 is mechanically chopped at a frequency \(f_1\), laser 2 is chopped at \(f_2\), and the photovoltage \(V\) is synchronously detected using a lock-in amplifier at the chopping difference frequency \(\Delta f \equiv f_1 - f_2\) (not to be confused with the heterodyne difference frequency). The resulting photovoltage \(V_\Delta \equiv V(I_1, I_2) - V(I_1, 0) - V(0, I_2)\) can be positive or negative, depending on the nonlinearity in the photothermal response. We also simultaneously measure the Fourier component at \(f_1\), denoted \(V_1 \equiv V(I_1, 0)\), which gives the photovoltage produced by laser 1 alone.

By simply comparing the magnitude of the two terms that compose the linearized cooling rate \(\gamma\), one can determine a condition for which process makes the largest contribution to the cooling rate. For nearly all of the experimental cases considered here and reported elsewhere, the cooling rate is largely limited by the supercollision term. Equation (3) reveals that despite this, the photoresponse can be either superlinear or sublinear in intensity, depending on the carrier density and graphene quality. As explained below, neither cooling effect can be ignored when analyzing the nonlinearity of the response.

When the heterodyne frequency exceeds the cooling rate (\(\Omega \gg \gamma\)), Eq. (2) simplifies to \(V(I) = a_1I + a_2I^2 - a_3I^3\), where \(I \equiv I_1 + I_2\) is the total absorbed optical intensity. The quadratic and cubic terms have opposite sign, and therefore describe superlinear or sublinear dependence on the optical intensity. From Eq. (3), one sees that the superlinear coefficient is proportional to \(\beta_1\), which we associate with momentum-conserving cooling, while the sublinear coefficient is proportional to \(\beta_3\), which arises from supercollision cooling.

Figure 2(a) plots \(V_1\) (black) and \(V_\Delta\) (green) as a function of the gate voltage for the HBN-encapsulated device. These measurements were performed with \(\Omega/2\pi = 2.5\) THz, which is much faster than the expected cooling rate at room temperature. The sign of the photothermal voltage \(V_1\) depends on the gate voltage, as expected from the photothermal effect [2,3,5]. For carrier densities near the

\[\text{FIG. 2. Photovoltage vs carrier concentration and incident power, measured at room temperature. (a) Single-laser photovoltage (\(V_1\)), and nonlinear photomixing signal (\(V_\Delta\)) measured vs the applied gate voltage \(V_g\). \(V_{\text{CNP}}\) denotes the charge neutral point. The red (\(V_1V_\Delta > 0\)) and blue (\(V_1V_\Delta < 0\)) regions indicate the conditions where super- and sublinear power dependence is observed. (b) Measured photovoltage \(V_1\) of a single laser vs incident optical power at two different gate voltages, showing sublinear and superlinear behavior. (c) Calculated photothermal voltage (in arbitrary units) vs input optical power for the case of \(\beta_1 = 0\) (blue) and \(\beta_3 = 0\) (red), illustrating the sublinear and superlinear behavior, respectively. Inset: energy diagram illustrating the two different cooling mechanisms.}\]
charge neutral point, $V_1$ and $V_\Delta$ have opposite sign (as indicated by the blue shading), revealing a sublinear power dependence, characteristic of supercollision cooling [7,13]. In this regime the Fermi surface is small, and the allowed phonon energy space for the momentum-conserving collision is strongly constrained, thereby suppressing conventional electron-phonon cooling [6,12]. At higher carrier densities, the behavior changes to superlinear (red shading), indicating that conventional cooling becomes stronger and dominates the photothermal nonlinearity. Figure 2(b) plots the single-beam photovoltage as a function of the incident optical power, confirming the sub- and superlinear behavior, respectively. Figure 2(c) illustrates the two cooling mechanisms schematically in $k$ space, along with the predicted sublinear and superlinear power dependence. The transitions outside of the Dirac cone represent supercollision cooling, in which the spatial disorder in the graphene compensates for the electron-phonon momentum mismatch.

The threshold between these two nonlinear regimes can be approximated by equating the opposing terms in $V_\Delta$, which gives

$$2a_1 \geq 3a_3 I,$$  \hspace{1cm} (4)

where the upper and lower inequalities describe the conditions under which conventional cooling or supercollision cooling prevails in the nonlinear response, respectively. The relative importance of the two competing cooling channels depends on temperature, intensity, the carrier concentration (Fermi level), and indirectly on the material quality, which is related to the disorder mean-free-path $l$. Even though the linearized cooling rate $\gamma$ is limited by supercollision cooling, both effects are evident in the nonlinear response reported here.

In the Supplemental Material (Ref. [33], Sec. S2), we present the results of a similar measurement performed on lower-mobility exfoliated graphene on SiO$_2$. Similar to the HBN-encapsulated device, we observe an expected transition from supercollision cooling to conventional cooling. The transition happens around $E_F = 80$ meV, and we use Eq. (4) to determine the ratio of the two rate coefficients, $\beta_1/\beta_3 = 5300$ K$^2$. At room temperature, the supercollision contribution to the cooling rate $\gamma$ is nearly $50\times$ larger than the contribution from conventional cooling. Despite this, both effects have a non-negligible role in the nonlinearity of the photoresponse, and their relative significance depends on the carrier density.

When the heterodyne difference frequency $\Omega$ is comparable to or smaller than the cooling rate $\gamma$, the electron temperature can follow the interferometric beating of the two lasers, which produces a larger photothermal voltage than when the lasers are widely detuned. The final two terms in Eq. (2) reveal that the nonlinear mixing signal $V_\Delta$ exhibits a Lorentzian dependence on the heterodyne difference frequency $\Omega$, with a spectral width that is proportional to the cooling rate $\gamma$. As before, the double-chopping configuration allows for sensitive detection of this heterodyne photomixing signal.

Figure 3(a) plots the measured photovoltage $V_\Delta$ as a function of the gate voltage and heterodyne difference frequency, for the nonencapsulated graphene detector. In addition to the expected gate-voltage dependence discussed previously, the photoresponse exhibits a distinct spectral peak around $\Omega = 0$. Figure 3(b) shows the photomixing spectrum at a fixed gate voltage, along with the best-fit Lorentzian curve. From the linewidth, we estimate a cooling time of $\gamma^{-1} = 1.42$ ps, which is consistent with the time-domain pulse coincidence measurements [5,37] reported for similar devices.

In order to confirm the thermal model for the photomixing, we repeated the heterodyne spectral measurements at temperatures from room temperature down to 25 K for the exfoliated sample on SiO$_2$ near the charge neutral point. As shown in Fig. 4(a), in all cases the photomixing signal exhibits a

![FIG. 3. Heterodyne photomixing response for the nonencapsulated device, measured at room temperature. (a) The nonlinear photomixing signal ($V_\Delta$) as a function of the difference frequency ($\Omega$) and gate voltage ($V_g$). At each gate voltage, $V_\Delta$ exhibits a Lorentzian-shaped dependence on the heterodyne difference frequency $\Omega$. (b) $V_\Delta$ vs $\Omega$ for $V_g = 4$ V. The dashed curve is the theoretical calculation of the photomixing voltage based on a photothermoelectric effect. From the Lorentzian fit, the hot electron cooling time is estimated to be $\gamma^{-1} = 1.42$ ps.](image)
ments reported elsewhere, the instantaneous absorbed intensity is orders of magnitude higher that the continuous-wave illumination considered here, in which case Eq. (4) predicts that supercollision cooling is the dominant contribution to the nonlinearity at all practically attainable doping concentrations. Moreover, nonencapsulated graphene samples have a much smaller disorder mean-free path $l$, which further contributes to the relative importance of supercollision cooling over conventional momentum-conserving cooling. In these cases, the photothermal response is often adequately described by supercollision cooling alone, for a wide range of carrier densities and temperatures [13,38,39]. For continuous-wave measurements on encapsulated devices, Eq. (4) also predicts that at sufficiently low temperatures, conventional cooling will prevail, consistent with temperature-dependent measurements reported recently [8].

We show that nonlinearity in the photothermoelectric effect causes photomixing when graphene is illuminated by near-infrared beams, and we describe a new heterodyne spectroscopy method that accurately measures this nonlinearity in the frequency domain. Exceedingly small nonlinearities in the photoresponse can be probed using continuous-wave illumination, which accurately elucidates the physical mechanisms behind the nonlinearity and cooling. In particular, the measurements reveal the role that disorder plays in the cooling of hot electrons, and the interplay of different cooling channels at different carrier concentrations. The method permits the direct measurement of the cooling rate in graphene using swept laser spectroscopy, which offers several advantages over pump-probe or pulse-coincidence measurements. The work also implies that nonlinear photomixing in graphene is very promising for the development of new optical and terahertz photomixing devices.

This work was sponsored by the U.S. ONR (N000141310865) and the U.S. NSF (ECCS 1309750). C. T. was supported by a DOD-AFOSR, NDSEG fellowship under Contract No. FA9550-11-C-0028, 32 CFR 168a. C. T. and J. H. acknowledge financial support from the Nanoelectronics Research Initiative (NRI) through the Institute for Nanoelectronics Discovery and Exploration (INDEX). K. W. and T. T. acknowledge support from the Elemental Strategy Initiative conducted by the MEXT, Japan and a Grant-in-Aid for Scientific Research on Innovative Areas “Science of Atomic Layers” from JSPS. M. S. F. was supported in part by an ARC Laureate Fellowship.

FIG. 4. Temperature dependence of the cooling rate. (a) The two-beam mixing signal as a function of the difference frequency measured close to the charge neutral point (sublinear power dependence regime) at different temperatures for the exfoliated sample on SiO$_2$. The dashed curves are Lorentzian fits. (b) The black circles are the extracted hot electron cooling time constant $\tau = \gamma^{-1}$ from the Lorentzian fits in panel (a). The blue (red) curve is the theory fit for the low (high) temperature.

Lorentzian spectral dependence, but with a spectral width that decreases with temperature, as expected. The solid blue curve in Fig. 4(b) shows a fit to the linearized cooling rate, based on the model presented here. For the data points above $T_L = 80$ K, and for the conditions at the charge neutral point, the assumption of $E_F \gg k_B T$ (degenerate regime) is no longer valid, which requires a modification of the cooling rate (Supplemental Material [33], Sec. S3). We therefore excluded these points when fitting the blue curve. However, when the parameters from the low-temperature fit were incorporated into the modified thermal model, it correctly predicts the observed high-temperature asymptotic behavior, indicated by the red curve, with no additional free parameters.

This nonlinear heterodyne photovoltage spectroscopy method has two important advantages over the traditional time-domain measurement using pulse coincidence [5,7,37]: (i) the frequency range and resolution is limited only by the tuning range and resolution of the laser, while in time-domain measurements the response is limited by the optical pulse width and repetition period; (ii) continuous-wave illumination produces a far smaller thermal stimulus to the graphene electrons than intense ultrafast pulses, thereby allowing the measurement of the temporal dynamics and nonlinearity of photodetection under low photothermal excitation for which the electron temperature is near the lattice temperature.

The model and measurements described here show that there are two competing cooling channels for hot electrons in graphene, and Eq. (4) describes the relative importance of each in the nonlinear response. In time-domain experiments reported elsewhere, the instantaneous absorbed

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